

$$\begin{aligned} f_r &= P[X = r] \\ &= \binom{a+r-1}{a-1} p^a (1-p)^r \\ &= p^a \frac{(a)_r}{r!} (1-p)^r, \quad r = 0, 1, \dots \end{aligned}$$